

TOPICS IN ALGEBRA

Part 1

RINGS AND REPRESENTATIONS OF ALGEBRAS

Editors of the Volume

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PREFACE

The 31st Semester “Classical Algebraic Structures” was held at the Stefan Banach International Mathematical Center in Warsaw from February 15 to June 15, 1988 and consisted of four sessions: The Theory of Rings (February 15–March 29), Representations of Finite-Dimensional Algebras and Related Topics (April 18–May 13), Commutative Algebra and Algebraic Geometry (April 5–16), Algebraic Groups, Their Combinatorics and Representations (May 15–June 15). The sessions were directed by Jan Krempa, Daniel Simson, Wolfgang Vogel and Tadeusz Józefiak respectively, and Stanisław Balcerzyk served as chairman of the Organizing Committee.

An International Conference on Representations of Algebras was held at the Banach Center from May 2 to May 7, 1988. It was partially supported by the Institute of Mathematics of the Nicholas Copernicus University in Toruń.

There were 244 participants of the Semester and 290 lectures were given by 139 lecturers. This volume contains some of the papers contributed to the first and second sessions of the Semester. The papers were accepted in final form by the editors before September 30, 1988 and are devoted mainly to group and semigroup algebras, forms of Hopf algebras, indecomposable representations of finite-dimensional algebras, Cohen–Macaulay modules, matrix problems, lattices over orders.

Papers contributed to the third and fourth sessions are published in part 2 of this volume, entitled “Topics in Algebra. Commutative Rings and Algebraic Groups”.

September, 1988

Editors

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