

## P R O B L È M E S

**P 416, R 1.** K. K. Kubota has constructed a series of counter-examples and proved that in the particular case, if at least one of the considered polynomials is injective, the answer is positive <sup>(1)</sup>. The latter result has been extended to polynomials of many variables by D. J. Lewis <sup>(2)</sup>.

X. 1, p. 187.

<sup>(1)</sup> K. K. Kubota, *Note on a conjecture of W. Narkiewicz*, Journal of Number Theory 4 (1972), p. 181-190.

<sup>(2)</sup> D. J. Lewis, *Invariant sets of morphisms on projective and affine number spaces*, Journal of Algebra 20 (1972), p. 419-434.

**P 744, R 1.** J. H. V. Hunt and E. D. Tymchatyn have informed us that they answered the problem by proving the following theorem:

*Let  $X$  be a Peano space which is expressible as a union of unicoherent regions  $U_1 \subset \bar{U}_1 \subset U_2 \subset \bar{U}_2 \subset \dots$  with compact closures. If  $A_1, A_2, \dots$  is a sequence of disjoint closed sets no one of which separates  $X$ , then  $X - \bigcup_{n=1}^{\infty} A_n$  is connected <sup>(3)</sup>.*

XXIII. 2, p. 326.

Letter of August 21, 1972.

<sup>(3)</sup> J. H. V. Hunt and E. D. Tymchatyn, *The theorem of Miss Mullikin-Mazurkiewicz - van Est for unicoherent Peano spaces*, Fundamenta Mathematicae 77 (1973), p. 285-287.

**P 749, R 1.** As Professor Roland E. Larson has observed <sup>(4)</sup>, the problem in the general case (i.e., for the lattice of all topologies) is easily answered in the affirmative by combining the two known results:

1. Any lattice is isomorphic to a sublattice of all equivalence relations on some set <sup>(5)</sup>.

<sup>(4)</sup> Letter of May 2, 1972.

<sup>(5)</sup> P. Whitman, *Lattices, equivalences relations, and subgroups*, Bulletin of the American Mathematical Society 52 (1946), p. 507-522.

2. The lattice of partition topologies on a set  $X$  is a sublattice of the lattice of all topologies on  $X$  <sup>(6)</sup>.

Using Larson's observation, Richard Valent shows in this fascicle <sup>(7)</sup> that the answer is affirmative also for the case of the lattice of all  $T_1$ -topologies on a set.

Independently, but also using Whitman's result <sup>(5)</sup>, Rosický has proved <sup>(8)</sup> that the answer remains affirmative even for the lattice of all completely Hausdorff topologies but fails for the lattice of all metrisable topologies.

XXIII. 2, p. 326.

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<sup>(6)</sup> R. Vaidyanathaswamy, *Treatise on set topology*, Indian Mathematical Society, Madras 1947.

<sup>(7)</sup> Richard Valent, *Every lattice is embeddable in the lattice of  $T_1$ -topologies*, this fascicle, p. 27-28.

<sup>(8)</sup> J. Rosický, *Embeddings of lattices in the lattice of topologies*, Archivum Mathematicum (Brno) (to appear).

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B. M. SCHEIN (SARATOV)

**P 850.** Formulé dans la communication *Compatible function semi-groups*.

Ce fascicule, p. 26.

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KAMIL D. JOSHI (BLOOMINGTON, INDIANA)

**P 851** et **P 852.** Formulés dans la communication *Characterizing plane ANR's by existence of local means*.

Ce fascicule, p. 44 et 46.

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K. M. GARG (EDMONTON, ALBERTA)

**P 853.** Formulé dans la communication *Monotonicity, continuity and levels of Darboux functions*.

Ce fascicule, p. 100.

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J. MUSIELAK (POZNAŃ)

**P 854.** Is the following conjecture true:

If a function  $x(t)$  defined in  $R^n$  has derivatives  $x^{(k)}(t)$ ,  $k = 0, 1, \dots$ ,

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belonging to  $L^p(-\infty, \infty)$ , where  $1 \leq p < \infty$ , then

$$\sup_k \int_{-\infty}^{\infty} |x^{(k)}(t)|^p dt < \infty$$

if and only if  $x(t)$  can be extended to an integer function of exponential type 1?

New Scottish Book, Probl. 875, 19. 5. 1972.

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H. J. BOTHE (BERLIN)

**P 855.** Let  $G$  be the complete graph with 6 vertices piecewise-linearly embedded in the euclidean 3-dimensional space. Are there two disjoint simple closed polygons in  $G$  which are linked homotopically (homologically)?

New Scottish Book, Probl. 876, 20. 5. 1972.

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